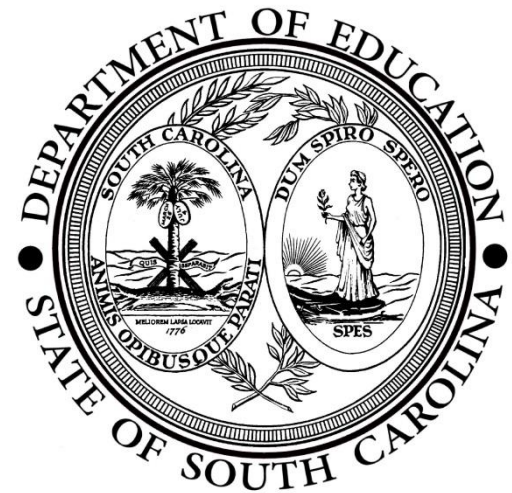


South Carolina College- and Career-Ready Standards for Mathematics 6th Grade Support Document

South Carolina Department of Education
Office of Standards and Learning
September 2015 - DRAFT



South Carolina College- and Career-Ready Standards for Mathematics Grade 6 Overview

The [Table of Contents](#) below arranges the [South Carolina College- and Career-Ready Standards for Mathematics](#) for middle school into *Course Coversheets* and *Units*.

- Each middle school *Course Coversheet* organizes the middle school course standards into possible instructional units and provides links to specific middle school course *Units*.
- Each middle school course *Unit* contains:
 - Clarifying notes related to the standards within the unit
 - New academic vocabulary in the unit
 - Prior and subsequent knowledge related to the unit
 - Description of the relationship between the standards in the unit
 - Potential instructional strategies and lessons
 - Resources for the unit
 - Sample formative assessment tasks and questions

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Unit	Standards	Support Document		
<u>Number System</u>	6.NS.1	Content Standards with Clarifying Notes	Prior Knowledge Required for this Unit	Potential Instructional Strategies/Lessons
	6.NS.2	New Academic Vocabulary	Subsequent Knowledge Related to this Unit	Resources
	6.NS.3		Relationship Among Standards in this Unit	Sample Formative Assessment Tasks/Questions
	6.NS.4 6.NS.9			
<u>Ratios and Rates</u>	6.RP.1	Content Standards with Clarifying Notes	Prior Knowledge Required for this Unit	Potential Instructional Strategies/Lessons
	6.RP.2	New Academic Vocabulary	Subsequent Knowledge Related to this Unit	Resources
	6.RP.3		Relationship Among Standards in this Unit	Sample Formative Assessment Tasks/Questions
<u>Graphing and Rational Numbers</u>	6.NS.5	Content Standards with Clarifying Notes	Prior Knowledge Required for this Unit	Potential Instructional Strategies/Lessons
	6.NS.6	New Academic Vocabulary	Subsequent Knowledge Related to this Unit	Resources
	6.NS.7		Relationship Among Standards in this Unit	Sample Formative Assessment Tasks/Questions
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<u>Expressions</u>	6.EE.1	Content Standards with Clarifying Notes	Prior Knowledge Required for this Unit	Potential Instructional Strategies/Lessons
	6.EE.2	New Academic Vocabulary	Subsequent Knowledge Related to this Unit	Resources
	6.EE.3		Relationship Among Standards in this Unit	Sample Formative Assessment Tasks/Questions
	6.EE.4			

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Equations	6.EE.5	Content Standards with Clarifying Notes	Prior Knowledge Required for this Unit	Potential Instructional Strategies/Lessons
	6.EE.6	New Academic Vocabulary	Subsequent Knowledge Related to this Unit	Resources
	6.EE.7		Relationship Among Standards in this Unit	Sample Formative Assessment Tasks/Questions
Statistics	6.DS.1	Content Standards with Clarifying Notes	Prior Knowledge Required for this Unit	Potential Instructional Strategies/Lessons
	6.DS.2	New Academic Vocabulary	Subsequent Knowledge Related to this Unit	Resources
	6.DS.3		Relationship Among Standards in this Unit	Sample Formative Assessment Tasks/Questions
Geometry	6.GM.1	Content Standards with Clarifying Notes	Prior Knowledge Required for this Unit	Potential Instructional Strategies/Lessons
	6.GM.2	New Academic Vocabulary	Subsequent Knowledge Related to this Unit	Resources
	6.GM.3		Relationship Among Standards in this Unit	Sample Formative Assessment Tasks/Questions

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Unit 1	Unit 2	Unit 3	Unit 4	Unit 5	Unit 6	Unit 7
Number System	Ratios and Rates	Graphing and Rational Numbers	Expressions	Equations	Statistics	Geometry
Standards	Standards	Standards	Standards	Standards	Standards	Standards
6.NS.1 6.NS.2 6.NS.3 6.NS.4 6.NS.9	6.RP.1 6.RP.2 6.RP.3	6.NS.5 6.NS.6 6.NS.7 6.NS.8	6.EE.1.1 6.EE.1.2 6.EE.1.3 6.EE.1.4	6.EE.1.5 6.EE.1.6 6.EE.1.7 6.EE.1.8 6.EE.1.9	6.DS.1 6.DS.2 6.DS.3 6.DS.4 6.DS.5	6.GM.1 6.GM.2 6.GM.3 6.GM.4

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Mathematical Process Standards: The South Carolina College- and Career-Ready (SCCCR) Mathematical Process Standards demonstrate the ways in which students develop conceptual understanding of mathematical content and apply mathematical skills. As a result, the SCCCR Mathematical Process Standards should be integrated within the SCCCR Content Standards for Mathematics for each grade level and course. Since the process standards drive the pedagogical component of teaching and serve as the means by which students should demonstrate understanding of the content standards, the process standards must be incorporated as an integral part of overall student expectations when assessing content understanding.

<p>1. Make sense of problems and persevere in solving them.</p> <ul style="list-style-type: none"> a. Relate a problem to prior knowledge. b. Recognize there may be multiple entry points to a problem and more than one path to a solution. c. Analyze what is given, what is not given, what is being asked, and what strategies are needed, and make an initial attempt to solve a problem. d. Evaluate the success of an approach to solve a problem and refine it if necessary. 	<p>5. Use a variety of mathematical tools effectively and strategically.</p> <ul style="list-style-type: none"> a. Select and use appropriate tools when solving a mathematical problem. b. Use technological tools and other external mathematical resources to explore and deepen understanding of concepts.
<p>2. Reason both contextually and abstractly.</p> <ul style="list-style-type: none"> a. Make sense of quantities and their relationships in mathematical and real-world situations. b. Describe a given situation using multiple mathematical representations. c. Translate among multiple mathematical representations and compare the meanings each representation conveys about the situation. d. Connect the meaning of mathematical operations to the context of a given situation. 	<p>6. Communicate mathematically and approach mathematical situations with precision.</p> <ul style="list-style-type: none"> a. Express numerical answers with the degree of precision appropriate for the context of a situation. b. Represent numbers in an appropriate form according to the context of the situation. c. Use appropriate and precise mathematical language. d. Use appropriate units, scales, and labels.
<p>3. Use critical thinking skills to justify mathematical reasoning and critique the reasoning of others.</p> <ul style="list-style-type: none"> a. Construct and justify a solution to a problem. b. Compare and discuss the validity of various reasoning strategies. c. Make conjectures and explore their validity. d. Reflect on and provide thoughtful responses to the reasoning of others. 	<p>7. Identify and utilize structure and patterns.</p> <ul style="list-style-type: none"> a. Recognize complex mathematical objects as being composed of more than one simple object. b. Recognize mathematical repetition in order to make generalizations. c. Look for structures to interpret meaning and develop solution strategies.
<p>4. Connect mathematical ideas and real-world situations through modeling.</p> <ul style="list-style-type: none"> a. Identify relevant quantities and develop a model to describe their relationships. b. Interpret mathematical models in the context of the situation. c. Make assumptions and estimates to simplify complicated situations. d. Evaluate the reasonableness of a model and refine if necessary. 	

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Unit Title
Number System
Content Standards with Clarifying Notes
<i>Open bullets indicate clarifying notes.</i>
<ul style="list-style-type: none"> ● 6.NS.1 Compute and represent quotients of positive fractions using a variety of procedures (e.g., visual models, equations, and real-world situations). <ul style="list-style-type: none"> ○ Divide positive fractions by fractions using visual models and equations. ○ Solve real-world problems using division of fractions. ● 6.NS.2 Fluently divide multi-digit whole numbers using a standard algorithmic approach. <ul style="list-style-type: none"> ○ Divide whole numbers by whole numbers ○ Convert remainders to fractional parts in simplest form and decimal notation ● 6.NS.3 Fluently add, subtract, multiply and divide multi-digit decimal numbers using a standard algorithmic approach. <ul style="list-style-type: none"> ○ Perform all operations with decimal notation ○ Modeling equivalent numerical expressions to support the understanding of division of decimal numbers ● 6.NS.4 Find common factors and multiples using two whole numbers. <ul style="list-style-type: none"> a. Compute the greatest common factor (GCF) of two numbers both less than or equal to 100. b. Compute the least common multiple (LCM) of two numbers both less than or equal to 12. c. Express sums of two whole numbers, each less than or equal to 100, using the distributive property to factor out a common factor of the original addends. ○ Understand that greatest common factor and least common multiple are ways to discuss number relationships in multiplication and division. ○ Understand the process of prime factorization. ○ Understand the distributive property using sums and its use in adding numbers 1-100 with a common factor. ○ Use LCM and GCF to teach fluency for adding and subtracting of fractions using a standard algorithmic approach. ● 6.NS.9 Investigate and translate among multiple representations of rational numbers (fractions, decimal numbers, percentages). Fractions should be limited to those with denominators of 2, 3, 4, 5, 8, 10, and 100. <ul style="list-style-type: none"> ○ Recognize $\frac{1}{8}$ as half of $\frac{1}{4}$ to assist with conversions within all representations. ○ Understand that fractions with a denominator of 3 will generate a repeating decimal (limit repeating decimals to fractions with a denominator of 3).

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New Academic Vocabulary for This Unit
<ul style="list-style-type: none">● Reciprocal● Inverse● Greatest common factor● Least common multiple● Prime factorization● Distributive property● Rational number

Prior Knowledge Required for this Unit
<ul style="list-style-type: none">● Multiplication facts (3.ATO.1, 3.ATO.3)● Understand the relationship between multiplication and division (5.NSF.3)● Understand parts of a fraction (3.NSF.1)● Divide up to four-digit dividends by two-digit divisors (5.NSBT.6)● Add, subtract, multiply, and divide decimal numbers to hundredths using concrete area models and drawings (5.NSBT.7)● Firm conceptual understanding of place value (3.NSBT.1, 4.NSBT.1, 5.NSBT.1)

Subsequent Knowledge Related to this Unit
<p>This unit will end direct instruction for operations with whole numbers, fractions, and decimals. To ensure readiness for work with integers in Grade 7, students must be computationally fluent with these operations. In Grade 8, students will be solving multi-step equations where the computational skills will be secondary skills in an algebraic approach. Students will begin multiple representations of rational numbers with limited denominators in Grade 6. That knowledge in Grades 7 and 8 will be extended to include all denominators and repeated decimals in Grade 8. The information taught in this unit will also prepare students for ratios and rates including work with greatest common factor and least common multiple for simplifying rates. This knowledge will be extended in Grade 8 to include work with functions including linear functions where students will analyze slope as the constant rate of change.</p>

Relationship Among Standards in this Unit
Standards in this unit are all necessary to develop computational skills necessary for work with positive rational numbers.

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Potential Instructional Strategies/Lessons

- Visual models - Multiple representations of visual models should be used to show multiplication and division of fractions.

Example 1:

Students understand that a division problem such as $3 \div \frac{2}{5}$ is asking, “how many $\frac{2}{5}$ are in 3?” One possible visual model would begin with three whole and divide each into fifths. There are 7 groups of two-fifths in the three wholes. However, one-fifth remains. Since one-fifth is half of a two-fifths group, there is a remainder of $\frac{1}{2}$.

Therefore, $3 \div \frac{2}{5} = 7\frac{1}{2}$, meaning there are $7\frac{1}{2}$ groups of two-fifths. Students interpret the solution, explaining how division by fifths can result in an answer with halves.



This section represents one-half of two-fifths

Students also write contextual problems for fraction division problems. For example, the problem, $\frac{2}{3} \div \frac{1}{6}$ can be illustrated with the following word problem:

Source: [NC DPI 6th Grade Mathematics Unpacked Contents](#)

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Example 2:

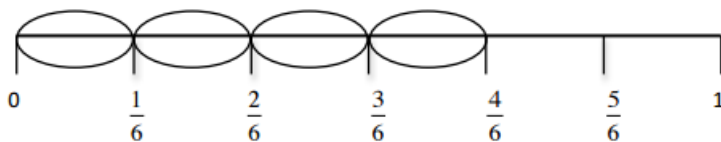
Susan has $\frac{2}{3}$ of an hour left to make cards. It takes her about $\frac{1}{6}$ of an hour to make each card. About how many can she make?

This problem can be modeled using a number line.

a. Start with a number line divided into thirds.



b. The problem wants to know how many sixths are in two-thirds. Divide each third in half to create sixths.



c. Each circled part represents $\frac{1}{6}$. There are four sixths in two-thirds; therefore, Susan can make 4 cards.

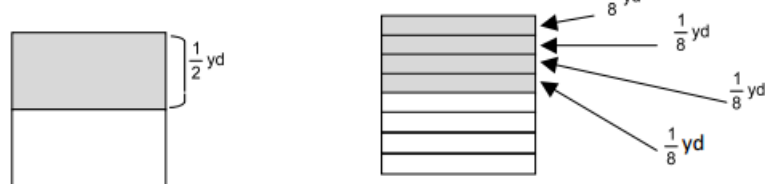
Source: [NC DPI 6th Grade Mathematics Unpacked Contents](#)

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Example 3:

Michael has $\frac{1}{2}$ of a yard of fabric to make book covers. Each book cover is made from $\frac{1}{8}$ of a yard of fabric. How many book covers can Michael make? Solution: Michael can make 4 book covers.



Example 4:

Represent $\frac{1}{2} \div \frac{2}{3}$ in a problem context and draw a model to show your solution.

Context: A recipe requires $\frac{2}{3}$ of a cup of yogurt. Rachel has $\frac{1}{2}$ of a cup of yogurt from a snack pack. How much of the recipe can Rachel make?

Explanation of Model:

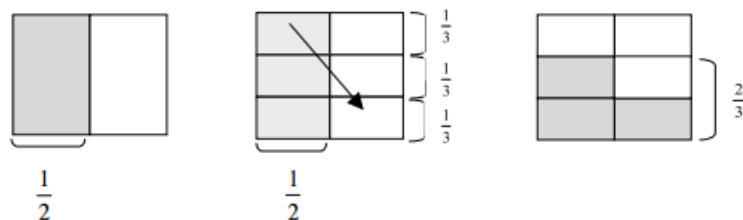
The first model shows $\frac{1}{2}$ cup. The shaded squares in all three models show the $\frac{1}{2}$ cup.

The second model shows $\frac{1}{2}$ cup and also shows $\frac{1}{3}$ cups horizontally.

The third model shows $\frac{1}{2}$ cup moved to fit in only the area shown by $\frac{2}{3}$ of the model.

$\frac{2}{3}$ is the new referent unit (whole).

3 out of the 4 squares in the $\frac{2}{3}$ portion are shaded. A $\frac{1}{2}$ cup is only $\frac{3}{4}$ of a $\frac{2}{3}$ cup portion, so only $\frac{3}{4}$ of the recipe can be made.



Source: [NC DPI 6th Grade Mathematics Unpacked Contents](#)

- Algorithmic approaches to divide multi-digit numbers
- Algorithmic approaches to add, subtract, multiply, and divide decimal numbers
- For division, modeling equivalent numerical expressions will support understanding of moving the decimal point

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- Prime factorization

Prime Factor Tree	
<ul style="list-style-type: none">• Start by dividing the given number by the smallest prime which is 2.• The factors of the number above are broken down into "branches" as indicated by the line segments.• We are able to divide 40 and its quotient by the prime number 2 three times which means this prime number will have an exponent of 3 in the factorization.• The last quotient after repeated division of 2 is a prime number which is 5.• Upon reaching a prime number as its last quotient in the process, this shows that we are done!	<p style="text-align: center;">$40 = 2 \times 2 \times 2 \times 5$ $= 2^3 \times 5$</p>

Source: [Chili Math](#)

- Upside Down Division (Birthday Cake)

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Upside-Down Division

- Now you know why it is called the Upside-Down Division because the division symbol is literally upside-down.



- I start dividing the given number by the smallest prime number which is 2. If that prime evenly divides the number, then I place the quotient below. Continue the process as needed.
- Notice that we are able to perform repeated division of prime number 2, until reaching the prime number 5 as its final whole number quotient (most bottom).
- Present the final factorization as product of exponential numbers having a prime number base in the exponential notation.

$$\begin{array}{r} \textcircled{2} \overline{) 40} \\ \underline{20} \\ \textcircled{2} \overline{) 20} \\ \underline{10} \\ \textcircled{2} \overline{) 10} \\ \underline{5} \\ \textcircled{5} \end{array}$$

$$\begin{aligned} 40 &= 2 \times 2 \times 2 \times 5 \\ &= 2^3 \times 5 \end{aligned}$$

Source: [Chili Math](#)

Resources

6.NS.1 - This game allows students to practice the division of fractions. <http://www.math-play.com/math-basketball-dividing-fractions-game/math-basketball-dividing-fractions-game.html>

6.NS.1 - This performance task requires students to divide fractions, interpret quotients, and support solutions. http://schools.nyc.gov/NR/ronlyres/946D93E8-E911-4589-871C-97317E227C3C/141874/NYCDOE_G6_Math_SharemyCandy_FINAL.pdf

6.NS.9 - The included activities encourage students to perform operations with fractions and translate between the multiple representations of rational numbers. http://empower.terc.edu/pdf/Using_Benchmarks.pdf

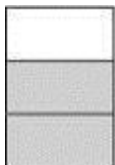
This website provides real-world problems associated with this unit. <https://www.illustrativemathematics.org/NS>

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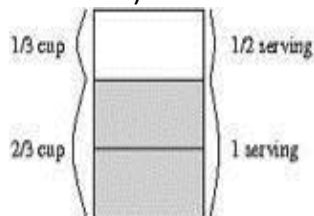
Sample Formative Assessment Tasks/Questions

Performance Task 6.NS.1: Tonya and Chrissy are trying to understand the following story problem for $1\div\frac{2}{3}$. *One serving of rice is $\frac{2}{3}$ of a cup. I ate 1 cup of rice. How many servings of rice did I eat?* To solve the problem, Tonya and Chrissy draw a diagram divided into three equal pieces, and shade two of those pieces.



Tonya says, "There is one $\frac{2}{3}$ -cup serving of rice in 1 cup, and there is $\frac{1}{3}$ cup of rice left over, so the answer should be $1\frac{1}{3}$." Chrissy says, "I heard someone say that the answer is $3/2=1\frac{1}{2}$. Which answer is right?" Is the answer $1\frac{1}{3}$ or $1\frac{1}{2}$? Explain your reasoning using the diagram.

Answer: In Tonya's solution of $1\frac{1}{3}$, she correctly notices that there is one $\frac{2}{3}$ cup serving of rice in 1 cup, and there is $\frac{1}{3}$ cup of rice left over. But she is mixing up the quantities of servings and cups in her answer. The question becomes how many servings is $\frac{1}{3}$ cup of rice? The answer is " $\frac{1}{3}$ cup of rice is $\frac{1}{2}$ of a serving." It would be correct to say, "There is one serving of rice with $\frac{1}{3}$ cup of rice left over," but to interpret the quotient $1\frac{1}{2}$ the units for the 1 and the units for the $\frac{1}{2}$ must be the same: *There are $1\frac{1}{2}$ servings in 1 cup of rice if each serving is $\frac{2}{3}$ cup.* (Source: Illustrative Mathematics)



Source: [Illustrative Mathematics](#)

Performance Task 6.NS.2: Southern Middle School is hosting a football game this Thursday. Band members are selling ads for the game's program. Their goal is to sell \$3,462 worth of ads. If the band members sell each ad for \$15, determine how many ads they will need to sell to reach their goal. Justify your answer.

Answer: 231 ads - To determine the number of ads to be sold, students should divide the cost of each ad (\$15) into the desired sells (\$3462). The resulting quotient is 230 with a remainder 12. Since the quotient is 230 with a remainder 12, students need to determine that 231 ads must be sold to reach the goal of \$3462 raised.

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Performance Task 6.NS.3: Jalyn and her 3 friends bought snacks that cost \$2.86, \$7.52, \$4.38, 2.95, and \$3.05. If they share the cost, how much will each student have to pay to divide it evenly?

Answer: \$5.23

Performance Task 6.NS.4b: Johnny and Maria like to go to the mall and window shop. Both Johnny and Maria are at the mall at the same time today. Johnny goes to the mall every 5 days while Maria goes to the mall every 6 days. When will Johnny and Maria run into one another again at the mall? (GCF)

Answer: 30 days

Performance Task 6.NS.4a,c: Bob scored 24 points in a basketball game while Jim scored 40 points. Write an equivalent numerical expression to find the sum of these two numbers. Justify your thinking.

Answer: $8(3 + 5)$ – To determine this answer the student needs to see that both 24 and 40 have a greatest common factor of 8. The student explains that factoring out the eight in both numbers allows them to write an equivalent expression using the distributive property. By factoring out the 8 you are left with adding 3 and 5 in the parentheses.

Performance Task 6.NS.9: Which form is best to use when comparing rational numbers? Explain your rationale.

Answer: Student answers will vary. Be sure their rationale supports the form they select.

Performance Task 6.NS.9: In this task, students are the head of a basketball team in the NBA. Their three best starters are injured and not available to play in the next game. It is now their task to look at the statistics provided, and decide which five players will start the game.



The Dream Team.pdf

Source: [Converting and Ordering Rational Numbers \[6th grade\]](#)

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Performance Task 6.NS.9: Before a game, Jake's batting average was exactly 0.350. That is the decimal representation for number of hits to number of times at bat. During the game, Jake bats 4 times and gets 2 hits. If Jake's batting average after the game is 0.359, how many times had Jake batted before the end of the game? Explain your reasoning.

Answer: 64 at bats after the game - To check Jake's batting average after the game with 2 hits in 4 at bats, you can take a row of numbers from the ratio table, add 2 to the first number and 4 to the second, and then evaluate the quotient. For example, if Jake had 7 hits in 20 at bats before the game, then we would have 9 hits in 24 at bats after the game. Since $9/24 = 3/8 = 0.375$, this is not the correct value. With 14 hits in 40 at bats, Jake would have 16 hits in 44 at bats for a batting average of $16/44 = 4/11 \approx 0.364$ so this is also not correct. With 21 hits in 60 at bats before the game, Jake would have 23 hits in 64 at bats after the game. Since $23/64 \approx 0.359$, this could be correct. The next value to calculate would be 28 hits in 80 at bats entering the game so 30 hits in 84 at bats after the game: $30/84 = 5/14 \approx 0.357$, so this is not correct. The more at bats Jake has before the game, the less impact his 2 hits in 4 at bats have on his overall batting average. The only possibility that fits the given information is that Jake had 21 hits in 60 at bats before the game therefore he had 64 at bats at the end of the game.

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Unit Title
Ratios and Rates
Content Standards with Clarifying Notes
<i>Open bullets indicate clarifying notes.</i>
<ul style="list-style-type: none"> ● 6.RP.1 Interpret the concept of a ratio as the relationship between two quantities, including part to part and part to whole. <ul style="list-style-type: none"> ○ Ratios compare two quantities ○ Simplify ratios to simplest form ● 6.RP.2 Investigate relationships between ratios and rates. <ul style="list-style-type: none"> a. Translate between multiple representations of ratios (i.e., a/b, $a : b$, a to b, visual models). b. Recognize that a rate is a type of ratio involving two different units. c. Convert from rates to unit rates. <ul style="list-style-type: none"> ○ When writing a ratio, order of terminology matters ○ Transfer between multiple representations of ratios ○ Understand that operations with ratios are generally performed when the ratio is written in fractional form ○ Exclude complex fractions (i.e. $\frac{1}{3} / 4$) ● 6.RP.3 Apply the concepts of ratios and rates to solve real-world and mathematical problems. <ul style="list-style-type: none"> a. Create a table consisting of equivalent ratios and plot the results on the coordinate plane. b. Use multiple representations, including tape diagrams, tables, double number lines, and equations, to find missing values of equivalent ratios. c. Use two tables to compare related ratios. d. Apply concepts of unit rate to solve problems, including unit pricing and constant speed. e. Understand that a percentage is a rate per 100 and use this to solve problems involving wholes, parts, and percentages. f. Solve one-step problems involving ratios and unit rates (e.g., dimensional analysis). <ul style="list-style-type: none"> ○ Ratios can be used to find missing values in a table ○ Percent is a rate per 100 ○ Ratio reasoning can be used to convert measurement units ○ Include single step dimensional analysis (e.g., converting miles to yards)

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New Academic Vocabulary for This Unit
<ul style="list-style-type: none">● Rate● Ratio● Unit Rate● Dimensional Analysis (single step)

Prior Knowledge Required for this Unit
<ul style="list-style-type: none">● Equivalent fractions (3.NSF.2, 4.NSF.1)● Simplifying fractions (3.NSF.2, 4.NSF.1)● Multiplication and division of rational numbers (5.NSF.4, 5.NSF.7)

Subsequent Knowledge Related to this Unit
<p>In Grade 5, students developed a conceptual understanding of writing equivalent fractions with unlike and like denominators using visual models. This knowledge will lead students to an understanding of how to simplify ratios and rates down to unit rates. Students will also need to build conceptual knowledge of rates and ratios due to the abstractness of comparing two things within a fraction. The comparison of two quantities with like units will lead students to an analysis of like and unlike units including complex fractions in Grade 7; additionally, students will extend their understanding to geometry by identifying the relationship between diameter and circumference. Work with ratios and rates will also contribute to students connecting this concept to probability, in Grade 7, by finding the number of like outcomes in a comparison with the number of total outcomes. Finding equivalent ratios using a table will lead students to finding a constant of proportionality in Grade 7 and ultimately the constant rate of change (slope) in Grade 8 Functions. In Grade 8, students will also explore transformations of transversals to transformations of similar figures including side lengths and angles.</p>

Relationship Among Standards in this Unit
Standards in this unit will establish an understanding of relationships that exist among quantities of similar and different units.

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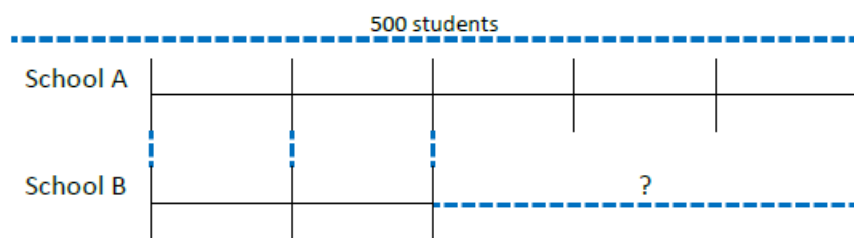
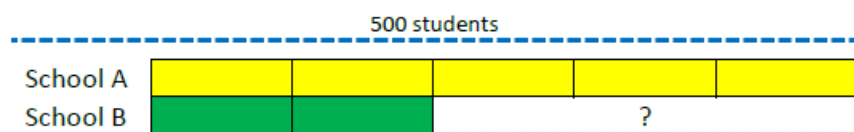
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Potential Instructional Strategies/Lessons

- **Visual Models** - Multiple representations of visual models should be used to show equivalencies among ratios and different missing values.

Tape diagrams

Comparison Model (part-part): School A has 500 students, which is $2\frac{1}{2}$ (which is equal to $\frac{5}{2}$) times as many students as School B. How many more students attend School A than School B?

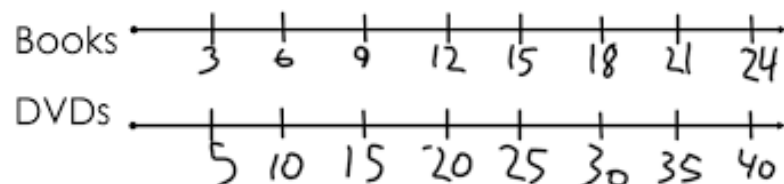


Tables

Girls	Boys
3	2
6	4
9	6
12	8

Double Number Lines

3 Books for every 5 DVDs



Equations

The equations generated during the ratio unit will be unique in that they follow the form of $y = mx$ or $px = q$ (these notations represent the same thing). The intercept (location the line crosses on the y-axis) will always be zero.

Miles traveled = $20 \cdot$ number of hours **or** $y = 20x$

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● **Dimensional Analysis Tables**

Starting amount	Equal amounts	End Amount
24 inches	1 foot	= feet
	12 inches	
24 inches	1 foot	= 2 feet
	12 inches	

Source: [Chemistry Land](#)

Resources

6.RP.2 - This video discusses the concepts of ratios, rates, and unit rates: <http://mathantics.com/index.php/section/lesson/ratiosandrates>

6.RP.2 - This site allows students to practice simplifying ratios and identifying equivalent ratios while racing a dirt bike around a track.
http://www.mathplayground.com/ASB_Index.html

6.RP. 3 - This task requires students to use proportional reasoning to compare the size of a typical hamburger with that of the largest hamburger ever made. <http://www.yummymath.com/2015/big-burger-2/>

6.RP.1-3 - This site includes a full lesson plan, activity instructions, and accompanying worksheets for ratio/rates competition stations.
<http://www.uen.org/Lessonplan/preview.cgi?LPid=23491>

Conceptual Foundations for Ratios and Proportions - <http://elemmath.jordandistrict.org/files/2012/06/CF1.docx>

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Sample Formative Assessment Tasks/Questions

Performance Task 6.RP.1: Pianos and pipe organs contain keyboards, a portion of which is shown below.



- a. What is the ratio of black keys to white keys in the picture above?
- b. If the pattern shown continues, how many black keys appear on a portable keyboard with 35 white keys?
- c. If the pattern shown continues, how many black keys appear on a pipe organ with a total of 240 keys?

Answers:

a. 5:7

b.

black keys	5	10	15	20	25
white keys	7	14	21	28	35

c.

black keys	5	10	100
total keys (black keys + white keys)	12	24	240

Source: [The New York City Department of Education](#)

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Performance Task 6.RP.2: There are 12 boys and 16 girls in a classroom. Which represents the simplified ratio of girls to students in the classroom?

- a. 3 to 4
- b. 4 to 3
- c. 4 to 7
- d. 7 to 4

Answer: C, to determine the answer to this question the students need to read the question and work left to right with setting up the ratio. The numerator of the ratio is 16 for girls and the denominator can be calculated by adding the number of boys and girls together to get 28. This gives me the ration $\frac{16}{28}$. I can simplify this down to $\frac{4}{7}$ by dividing by the greatest common factor of 4.

Performance Task 6.RP.3: Dianne went for a ride on her new scooter. She traveled 450 meters in 36 seconds. Which statements are true? Select all that apply.

- a. She traveled 12.5 meters every second.
- b. Every 75 seconds she traveled 6 meters.
- c. Every 8 seconds she traveled 100 meters.
- d. She traveled 1 meter in 0.8 second.
- e. Every 24 seconds, she traveled 300 meters.

Answer: A, C, E - To determine the answer to this question, students must determine the unit rate that represents Dianne's speed. Since she is traveling at a rate of 12.5 meters for every one second, answer choice A is correct. Answer choice B is incorrect because it did not maintain the correct order in the ratio; it would be 75 meters for every 6 seconds. Answer choice C is correct because 12.5 meters multiplied by 8 is 100 meters, and 1 second multiplied by 8 is 8 seconds. By multiplying each part of the rate by the same factor we maintain an equivalent ratio. Answer choice D is incorrect because the rate was simplified incorrectly. A correct statement would read that, "She traveled 1 meter in 0.08 seconds." Answer choice E is correct because 12.5 meters multiplied by 24 is 300 meters, and 1 second multiplied by 24 is 24 seconds.

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Performance Task 6.RP.1: This task requires students to use their knowledge of elapsed time and proportional reasoning to answer questions about record setting sporting events.



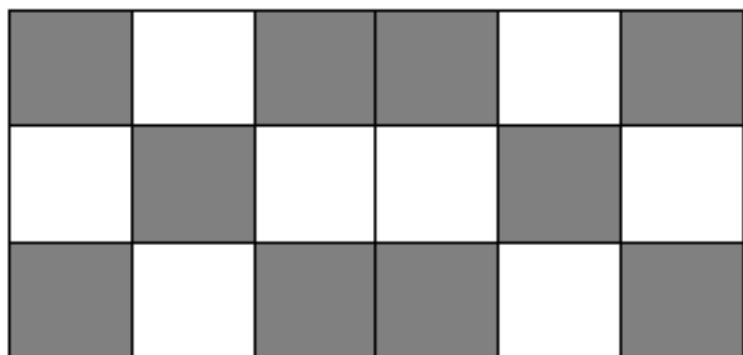
Longest_NHL_Matche
s_Ever.pdf

Source: [Yummy Math](#)

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Performance Task 6.RP.1 and 6.RP.2: The new floor in the school cafeteria is going to be constructed of square tiles that are either gray or white and in the pattern that appears below:



Part A: What is the ratio of gray tiles to white tiles?

Answer: _____

Part B: What is the ratio of white tiles to the total number of tiles in the pattern?

Answer: _____

Part C: If the total cost of the white tiles is \$12, what is the unit cost per white tile?

Answer: \$ _____

Answer:

Part A: 10 to 8, 5:4, or other equivalent ratio. The correct answer is a ratio of 10 gray tiles to 8 white tiles, or simplified, the ratio will be 5 gray tiles to 4 white tiles.

Part B: 8 to 18, 4:9, or other equivalent ratio. The correct answer is a ratio of 8 white tiles to 18 total tiles, or simplified, the ratio will be 4 white tiles to 9 tiles, in total.

Part C: \$1.50 per white tile. Counting the tiles by color in the pattern above, it is found that there are 8 white tiles. If 8 white tiles cost \$12, then the cost per white tile is \$1.50.